

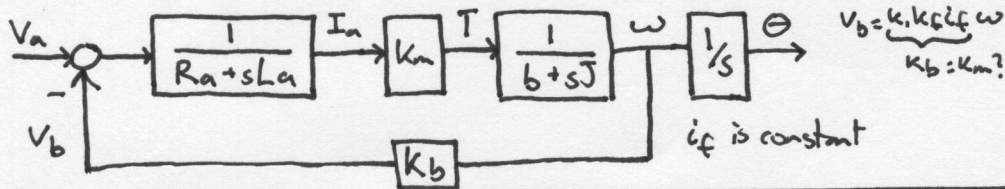
$V = Ri$ $f = by' = bv$
 $L \frac{di}{dt} = V$ $f = ky = k \int v dt$
 $C \frac{dV}{dt} = i$ $F = M \frac{d^2 y}{dt^2} = M \frac{dv}{dt}$

$F(s) = \int_{-\infty}^{\infty} f(t) e^{-st} dt$
 $f(t) = \int_{-\infty}^{\infty} F(s) e^{st} dt$
 $u(t) \rightarrow \frac{1}{s}$ $\mathcal{L}(f'(t)) = sF(s) - f(0)$
 $e^{-at} \rightarrow \frac{1}{s+a}$ $\mathcal{L}(f''(t)) = s^2 F(s) - sf(0) - f'(0)$
 $\delta(t) \rightarrow 1$ $\sin \omega t = \frac{\omega}{s^2 + \omega^2}$
 $\checkmark \rightarrow \frac{1}{s^2}$ $\cos \omega t = \frac{s}{s^2 + \omega^2}$



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1st Order System and Step Response:

$\frac{K}{Ts+1}$, at $t=T$, Amplitude is $0.63K$

Routh-Hurwitz: In first column can have no zeros, no sign changes

$\frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2}$

$\zeta > 1$, overdamped (2 real roots)
 $\zeta = 1$, critically damped (2 at same spot)
 $\zeta < 1$, underdamped (complex conjugates)

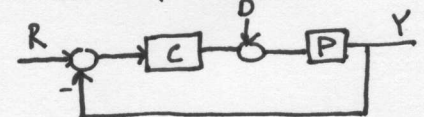
p.o. = $\exp\left\{\frac{-\zeta\pi}{\sqrt{1-\zeta^2}}\right\}$

$T_p = \frac{\pi}{\omega_n \sqrt{1-\zeta^2}}$ $\zeta = 2\%, T_s = \frac{4}{\zeta\omega_n}$
 $\zeta = 5\%, T_s = \frac{3}{\zeta\omega_n}$

$\zeta = \frac{\ln(p.o.)}{\sqrt{\pi^2 + \ln^2(p.o.)}}$

$T_s = \frac{-\ln(\zeta) + \frac{1}{2}\ln(1-\zeta^2)}{\zeta\omega_n}$

Closed Loop Stability:



Stable if all $\{R, D\}$ to $\{X, Y\}$ are stable

Sensitivity: $ST_P = \frac{P}{T} \left(\frac{\partial T}{\partial P} \right)$

Steady State Error: $K_p = \lim_{s \rightarrow 0} G(s)$



$K_v = \lim_{s \rightarrow 0} sG(s)$

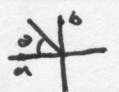
type 0 Unit Step $1/(1+K_p)$
 type 1 0
 type 2 0

Ramp ∞
 $1/K_v$
 0

e_{ss}

$s = \frac{-5 \pm \sqrt{b^2 - 4ac}}{2a}$

$\Theta = a \cos(\zeta)$
 $a = \zeta\omega_n$



$\frac{s+1}{s^2+s+1} = \frac{A}{s} + \frac{Bs+C}{s^2+s+1}$

Multiply through by (2), solve for A, B, C = 1, -1, 0

$\therefore \frac{1}{s} = \frac{s}{s^2+s+1}$

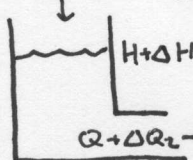
$\frac{s}{s^2+s+1} = \frac{D}{s + \frac{1}{2} + j\frac{\sqrt{3}}{2}} + \frac{E}{s + \frac{1}{2} - j\frac{\sqrt{3}}{2}}$

solve for D and E

$\Delta Q_1 - \Delta Q_2 = A \frac{d\Delta H}{dt}$

$\Delta Q_2 = \left. \frac{dQ_2}{dH} \right|_{H=H_0} \Delta H$

$Q_1 + \Delta Q_1$ $Q_1 = Q_2 = f(H)$



Linear Approximation:

ex: $Q = K(P_1 - P_2)^{1/2}$

$\Delta Q = \frac{dQ}{dP_1} \Delta P_1 + \frac{dQ}{dP_2} \Delta P_2$ Note: $\frac{dP_1}{dP_1} = \Delta P_1$

$\therefore \Delta Q = \frac{K}{2(P_1 - P_2)^{1/2}} (\Delta P_1 - \Delta P_2)$

$\zeta \leq \frac{\ln \zeta}{T_s} \pm \frac{\pi}{T_p}$ $\zeta = \omega_n \sqrt{1-\zeta^2}$

Mason's Formula:

$\frac{Y}{R} = \frac{\sum P_k \Delta_k}{\Delta}$

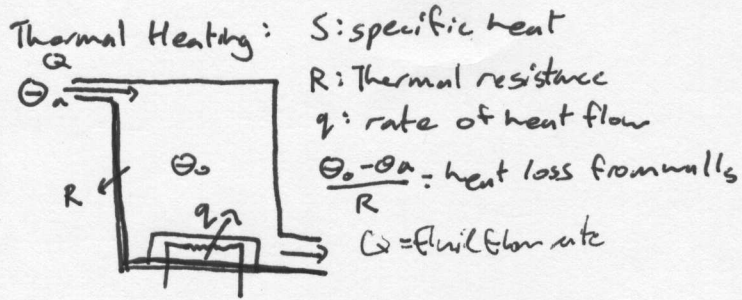
$\Delta = 1 - \sum \text{all loop gains}$

+ $\sum \text{all loop gain products}$
of 2 non-touching loops

- $\sum \text{all } \dots 3 \dots$

+ ...

$\Delta_k = \Delta$ when kth path is eliminated



$$\frac{Y}{R} = \frac{CP}{1+LP} \quad \frac{Y}{D} = \frac{P}{1+LP} \quad \frac{X}{D} = \frac{-PL}{1+LP}$$

$$QS\Theta_o - QS\Theta_a = \text{heat going out} = QS(\Theta_o - \Theta_a)$$

$$\therefore q - QS(\Theta_o - \Theta_a) - \frac{(\Theta_o - \Theta_a)}{R} = C_s \frac{d\Theta(t)}{dt}$$

solve for q , then \int

Note $\Theta(t) \rightarrow \Theta(s)$

$(\Theta_o - \Theta_a) = \Theta(t) \rightarrow \Theta(s)$

$$\frac{\Theta(s)}{1(s)} = -$$

$\frac{d\Theta}{dt}$ rate of heat change
 thermal capacitance